


Chapter 3

Kinematics in Two Dimensions; Vectors

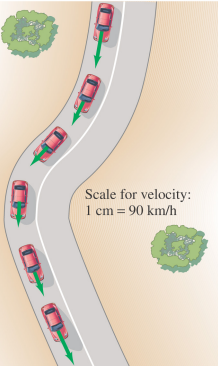


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Units of Chapter 3

- Vectors and Scalars
- Addition of Vectors – Graphical Methods
- Subtraction of Vectors, and Multiplication of a Vector by a Scalar
- Adding Vectors by Components
- Projectile Motion
- Solving Problems Involving Projectile Motion
- Projectile Motion Is Parabolic
- Relative Velocity

3-1 Vectors and Scalars



A vector has magnitude as well as direction.

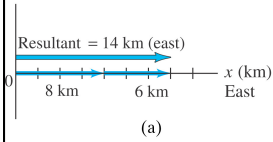
Some vector quantities: displacement, velocity, force, momentum

A scalar has only a magnitude.

Some scalar quantities: mass, time, temperature

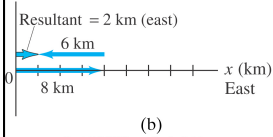
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3-2 Addition of Vectors – Graphical Methods



For vectors in one dimension, simple addition and subtraction are all that is needed.

You do need to be careful about the signs, as the figure indicates.

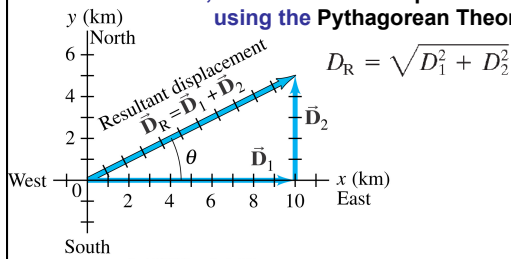


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3-2 Addition of Vectors – Graphical Methods

If the motion is in two dimensions, the situation is somewhat more complicated.

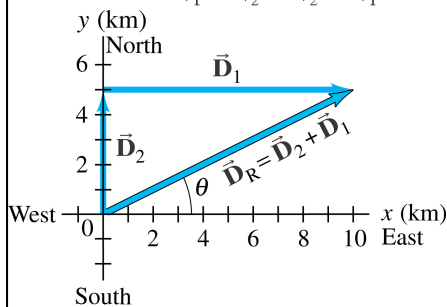
Here, the actual travel paths are at right angles to one another; we can find the displacement by using the Pythagorean Theorem.



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3-2 Addition of Vectors – Graphical Methods

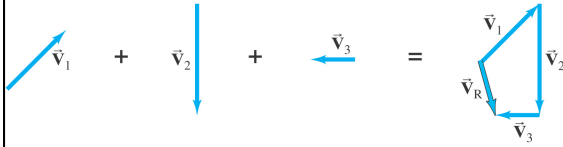
Adding the vectors in the opposite order gives the same result: $\vec{v}_1 + \vec{v}_2 = \vec{v}_2 + \vec{v}_1$



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3-2 Addition of Vectors – Graphical Methods

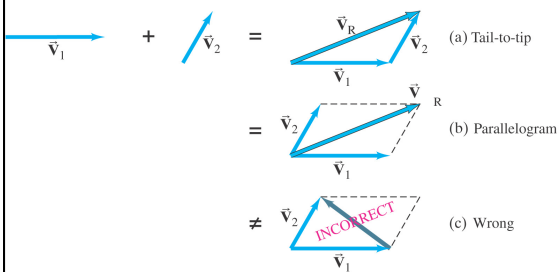
Even if the vectors are not at right angles, they can be added graphically by using the “tail-to-tip” method.



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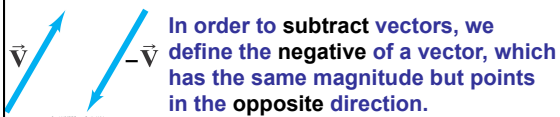
3-2 Addition of Vectors – Graphical Methods

The parallelogram method may also be used; here again the vectors must be “tail-to-tip.”



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3-3 Subtraction of Vectors, and Multiplication of a Vector by a Scalar



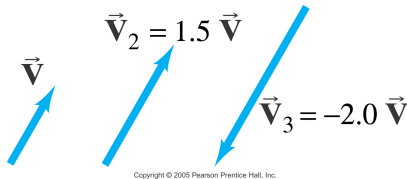
Then we add the negative vector:



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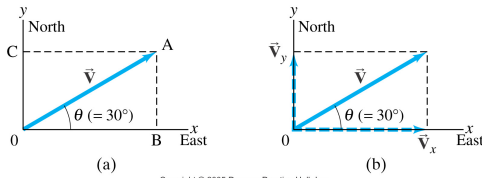
3-3 Subtraction of Vectors, and Multiplication of a Vector by a Scalar

A vector \vec{V} can be multiplied by a **scalar** c ; the result is a vector $c\vec{V}$ that has the same **direction** but a **magnitude** cV . If c is **negative**, the resultant vector points in the opposite direction.

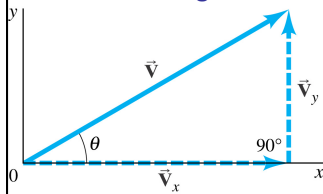


3-4 Adding Vectors by Components

Any vector can be expressed as the **sum** of two other vectors, which are called its **components**. Usually the other vectors are chosen so that they are **perpendicular** to each other.



3-4 Adding Vectors by Components



$$\sin \theta = \frac{V_y}{V}$$

$$\cos \theta = \frac{V_x}{V}$$

$$\tan \theta = \frac{V_y}{V_x}$$

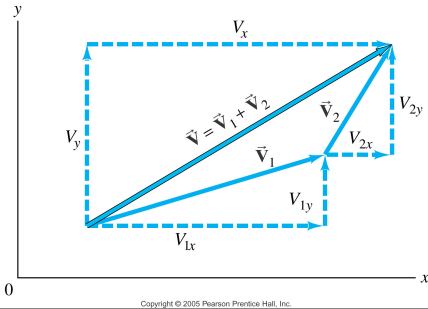
$$V^2 = V_x^2 + V_y^2$$

If the components are **perpendicular**, they can be found using **trigonometric functions**.

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3-4 Adding Vectors by Components

The **components** are effectively one-dimensional, so they can be added **arithmetically**:



3-4 Adding Vectors by Components

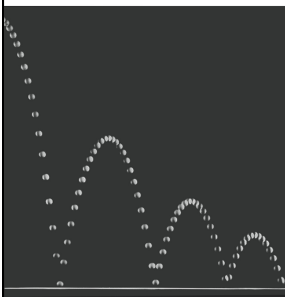
Adding vectors:

1. Draw a diagram; add the vectors graphically.
2. Choose **x** and **y** axes.
3. Resolve each vector into **x** and **y** components.
4. Calculate each component using sines and cosines.
5. Add the components in each direction.
6. To find the length and direction of the vector, use:

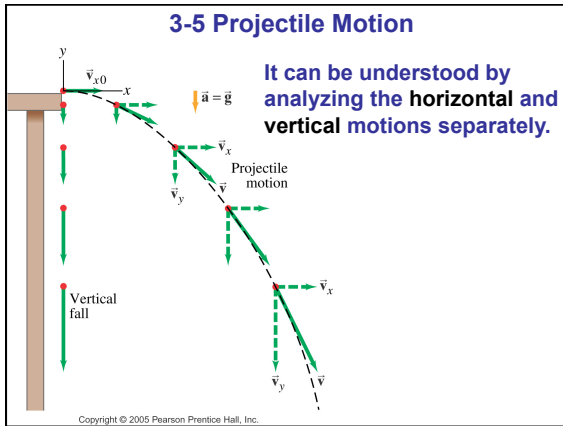
$$V = \sqrt{V_x^2 + V_y^2}$$

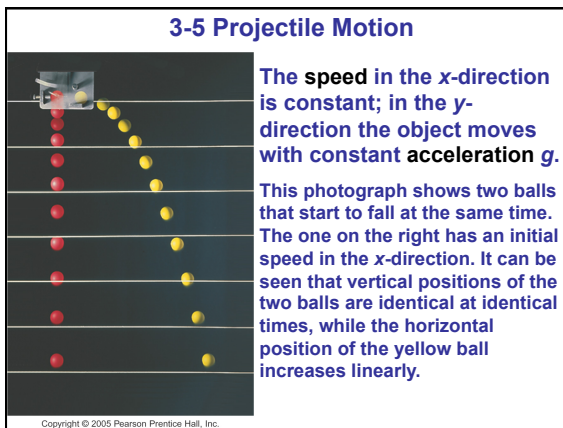
$$\tan \theta = \frac{V_y}{V_x}$$

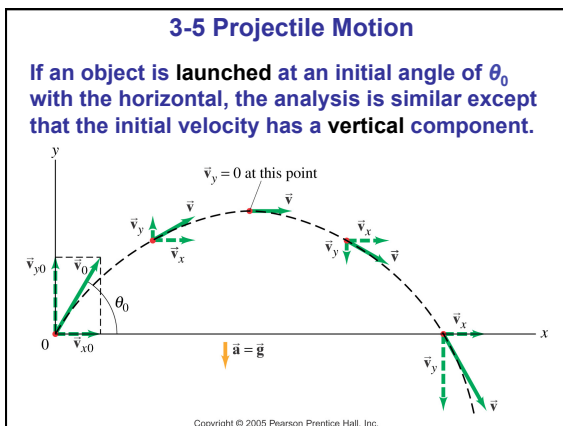
3-5 Projectile Motion



A **projectile** is an object moving in two dimensions under the influence of Earth's gravity; its path is a parabola.







3-6 Solving Problems Involving Projectile Motion

Projectile motion is motion with constant acceleration in two dimensions, where the acceleration is g and is down.

TABLE 3-2 Kinematic Equations for Projectile Motion
(y positive upward; $a_x = 0$, $a_y = -g = -9.80 \text{ m/s}^2$)

Horizontal Motion ($a_x = 0$, $v_x = \text{constant}$)	V	Vertical Motion [†] ($a_y = -g = \text{constant}$)
$v_x = v_{x0}$	(Eq. 2-11a)	$v_y = v_{y0} - gt$
$x = x_0 + v_{x0}t$	(Eq. 2-11b)	$y = y_0 + v_{y0}t - \frac{1}{2}gt^2$
	(Eq. 2-11c)	$v_y^2 = v_{y0}^2 - 2g(y - y_0)$

[†]If y is taken positive downward, the minus ($-$) signs in front of g become $+$ signs.

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3-6 Solving Problems Involving Projectile Motion

1. Read the problem carefully, and choose the object(s) you are going to analyze.
2. Draw a diagram.
3. Choose an origin and a coordinate system.
4. Decide on the time interval; this is the same in both directions, and includes only the time the object is moving with constant acceleration g .
5. Examine the x and y motions separately.

3-6 Solving Problems Involving Projectile Motion

6. List known and unknown quantities. Remember that v_x never changes, and that $v_y = 0$ at the highest point.
7. Plan how you will proceed. Use the appropriate equations; you may have to combine some of them.

3-7 Projectile Motion Is Parabolic



In order to demonstrate that projectile motion is **parabolic**, we need to write y as a function of x . When we do, we find that it has the form: $y = Ax - Bx^2$



This is indeed the equation for a parabola.

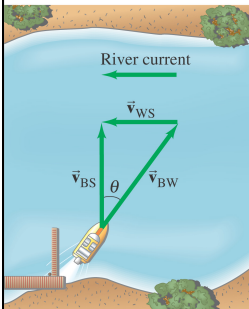
3-8 Relative Velocity

We already considered **relative speed** in one dimension; it is similar in two dimensions except that we must add and subtract velocities as **vectors**.

Each velocity is labeled first with the **object**, and second with the reference **frame** in which it has this velocity. Therefore, v_{WS} is the velocity of the water in the shore frame, v_{BS} is the velocity of the boat in the shore frame, and v_{BW} is the velocity of the boat in the water frame.

3-8 Relative Velocity

In this case, the relationship between the three velocities is:



$$\vec{v}_{BS} = \vec{v}_{BW} + \vec{v}_{WS} \quad (3-6)$$

Summary of Chapter 3

- A quantity with magnitude and direction is a vector.
- A quantity with magnitude but no direction is a scalar.
- Vector addition can be done either graphically or using components.
- The sum is called the resultant vector.
- Projectile motion is the motion of an object near the Earth's surface under the influence of gravity.
